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# The coolant penetration in grinding with a segmented wheel—Part 2: Quantitative analysis

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# Abstract

This paper develops a quantitative model to predict the power of coolant penetration into the grinding zone of a segmented wheel. The model accounts for the coolant properties and system design characteristics governing the penetration mechanism revealed by the theory established in Part 1 of this series study. By coupling with the author's previous mist formation analysis, the model offers a quantitative control guideline for the optimal use of grinding coolants.

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Keywords: Coolant; Optimisation; Quantitative model; Segmented grinding wheel; Mist formation

# 1. Introduction

Thermal damage is one of the major problems in grinding where a workpiece experiences heating within a small wheel-workpiece contact zone. Therefore, rapid convective heat dissipation within the zone is essential and it greatly depends on the quantity of coolant which can penetrate into the zone [1]. An understanding of the coolant penetration mechanism is therefore of particular importance in the development of an advanced coolant supply system. In Part 1 of this series study [2], the authors have explored the mechanisms of coolant penetration when using a conventional and a segmented wheel in surface grinding. It was found that unlike the conventional wheel, the segmented wheel possesses a higher pumping power when the wheel speed increases, and that the magnitude of the pumping power enhancement depends on the sum of velocities of the coolant jets. The significance in coolant minimisation [3] was qualitatively explained and proved to be possible under certain conditions, particularly when a pressurised coolant chamber was used. However, it must be emphasised that in practice, such applications usually involve complex flow

geometries of the coolant jets influenced by two motions, the grinding wheel rotation and the coolant's radial motion [4]. These effects will significantly alter the development of the coolant velocity profile [5–8] which is a function of the grinding system configuration, total quantity of coolant supplied to the system and the viscous properties of coolant.

On the other hand, because of the interfacial instability, high speed coolant jets are more susceptibly disintegrated into drops [6,7]. The efforts to enhance the pumping power by simply increasing the jet velocity will raise the mist formation rate, as pointed out by the authors [4]. As these drops are intrusive to environment of manufacturing [9], a better solution for high pumping power must be associated with the environmental consciousness.

While the analytical modelling in Part 1 of this series study [2] reveals the mechanism of pumping power qualitatively, it is hard to produce a quantitative prediction with sufficient accuracy which is of great importance in practice. It is noticed that dimensional analysis can often give very satisfactory formulae for quantitative prediction, particularly when it is used in conjunction with an analytical model [10–16]. Thus, this paper will conduct a quantitative analysis of the pumping power to develop a guideline for the optimal use of coolant. The experimental setup is the same as in Part 1 of the series study [2]. The coolant jet velocity is determined by the method of high-speed strobe photography (see the Appendix for details).

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$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	Nomen	Nomenclature							
bwheel width (m)Re ccritical Reynolds number, Eq. (A5)binner coolant chamber width (m) $v_{1k}$ velocity of a coolant jet (m/s)bmemory color more wheel in width (m) $v_{1k}$ velocity of a coolant jet (m/s)CmCpdimensionless correlation coefficient (1/m <sup>4</sup> ) $v_{1k}$ welve number, $(A2)$ , $(\rho v_{k}^2 d/\sigma)$ Crcoolant chamber characteristic coefficient (1/m <sup>4</sup> ) $\Delta p$ pressure drop $\Delta p$ Crcoolant chamber characteristic coefficient (1/m <sup>4</sup> ) $\Delta p$ preforated hole length shown in Fig. 3 (m)Crcoefficient in Eq. (2) (m <sup>2</sup> ) $\Delta p$ perforated hole diameter (m)d <sub>h</sub> perforated hole diameter (m) $\Delta m$ perforated hole diameter (m)d <sub>h</sub> centrifugal force acting on a unit volume of coolant (N/m <sup>3</sup> ) $\sigma$ control volume angle (rad)ggravitational constant (m/s <sup>2</sup> ) $\rho$ coolant density (kg/m <sup>3</sup> )hequivalent liquid layer thickness in Eq. (2) (m) $\rho_a$ density of chemical additives (kg/m <sup>3</sup> )htotal number of segments in a segmented wheel nchamber (Fig. 5) $\omega$ maxsafety limit of grinding wheel speed (rad/s)OESoccupational exposure standard (kg/m <sup>3</sup> ) $\omega$ safety limit of grinding wheel speed (rad/s)Ppumping power (W) $\mu$ , $r$ correlation power factors $m, n, q, r$ correlation power factorsPpower number, $(P/\rho R^5 \omega^3)$ hperforated hole of the segmented wheel $n, n, q, r$ correlation power factors $m, n, q, r$ correlation power factors <th>Α</th> <th>area (m<sup>2</sup>)</th> <th>Re<sub>1</sub></th> <th>Reynolds number, Eq. (A4), <math>(\rho v_{ik} d_l/\mu)</math></th>	Α	area (m <sup>2</sup> )	Re <sub>1</sub>	Reynolds number, Eq. (A4), $(\rho v_{ik} d_l/\mu)$					
$b_{ch}$ inner coolant chamber width (m) $v_{ik}$ velocity of a coolant jet (m/s) $b_r$ inner whele rim width (m) $v_{ik}$ velocity of a coolant jet (m/s) $b_r$ inner whele rim width (m) $w_{ik}$ Weer number, $(\rho R^{b} o^{2}/\sigma)$ $C_m$ coolant chamber characteristic coefficient $dp$ pressure drop $(1/1)$ and (21), respectively $dp$ pressure drop through the perforate $C_{rw}$ dimensionless geometrical influence number $dp$ pressure drop through the perforate $C_{rw}$ coefficient in Eq. (2) (m <sup>2</sup> ) $dp$ mean static pressure drop through the perforate $d_h$ perforated hole diameter (m) $dp$ means static pressure drop through the perforate $d_h$ perforated hole diameter of a liquid jet in Eq. (A1) (m) $\gamma$ control volume angle (rad) $f_c$ centrifugal force acting on a unit volume of $(kg/m^3)$ $\rho_a$ $g$ gravitational constant (m/s <sup>2</sup> ) $\rho_a$ density of chemical additives (kg/m <sup>3</sup> ) $h$ equivalent liquid jet in Eq. (A1) (m) $\sigma$ surface tension (N/m) $N$ total number of segments in a segmented wheel $(rad)$ $n_{ch}$ number of perforated holes within the coolant $\sigma$ $n_{ch}$ number, ( $P/\rho R^5 \omega^3$ ) $\omega_{max}$ safety limit of grinding wheel speed (rad/s) $OES$ occupational exposure standard (kg/m <sup>3</sup> ) $\omega_{max}$ safety limit of grinding wheel speed (rad/s) $p$ pressure (Pa) $\omega_{max}$ safety limit of grinding wheel speed (rad/s) $Q^*$ flow ra	b	wheel width (m)	-						
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$ \begin{array}{cccc} C_{\rm nv} C_{\rm p} & {\rm dimensionless correlation coefficients in Eqs.} \\ (17) and (21), respectively \\ C_{\rm f} & {\rm coolant chamber characteristic coefficient} \\ (1/m^4) \\ C_{\rm s} & {\rm coefficient in Eq. (2) (m^2)} \\ A_{\rm p} & {\rm pressure drop} \\ C_{\rm fw} & {\rm dimensionless geometrical influence number} \\ C_{\rm fw} & {\rm dimensionless geometrical influence number} \\ C_{\rm fw} & {\rm dimensionless geometrical influence number} \\ A_{\rm h} & {\rm perforated hole lameter (m)} \\ A_{\rm d} & {\rm break-up diameter of a liquid jet in Eq. (A1) (m)} \\ f_{\rm c} & {\rm centrifugal force acting on a unit volume of} \\ {\rm coolant (N/m^3)} \\ g & {\rm gravitational constant (m/s^2)} \\ h & {\rm equivalent liquid layer thickness in Eq. (2) (m)} \\ l & {\rm break-up length of a liquid jet in Eq. (A1) (m)} \\ N & {\rm total number of gerforated holes within the coolant} \\ {\rm chamber (Fig. 5)} \\ Oh & Ohnesorge number, (Eq. (A3), (Oh = \mu/(\rho\sigma d_1)^{0.5}) \\ P & {\rm pumping power (W)} \\ P^* & {\rm power number, Eq. (21), (Q/R^3\omega)} \\ Q_{\rm m} & {\rm mist flow rate (m^3/s)} \\ Q_{\rm m} & {\rm mist flow rate (m^3/s)} \\ Q_{\rm m} & {\rm mist flow rate (m^3/s)} \\ Q_{\rm min} & {\rm minimum coolant flow rate required in Eq. (27)} \\ (m^3/s) \\ Q_{\rm min} & {\rm minimum coolant flow rate required in Eq. (27)} \\ (m^3/s) \\ Q_{\rm min} & {\rm minimum coolant flow rate required in Eq. (27)} \\ (m^3/s) \\ Q_{\rm min} & {\rm minimum coolant flow rate required in Eq. (27)} \\ (m^3/s) \\ Q_{\rm min} & {\rm minimum coolant flow rate required in Eq. (27)} \\ (m^3/s) \\ Q_{\rm min} & {\rm minimum coolant flow rate required in Eq. (27)} \\ (m^3/s) \\ Q_{\rm min} & {\rm minimum coolant flow rate required in Eq. (27)} \\ (m^3/s) \\ Q_{\rm min} & {\rm minimum coolant flow rate required in Eq. (27)} \\ (m^3/s) \\ Q_{\rm min} & {\rm minimum coolant flow rate required in Eq. (27)} \\ (m^3/s) \\ Q_{\rm min} & {\rm minimum coolant flow rate required in Eq. (27)} \\ (m^3/s) \\ Q_{\rm min} & {\rm minimum coolant flow rate required in Eq. (27)} \\ (m^3/s) \\ Q_{\rm min} & {\rm minimum coolant flow rate required in Eq. (27)} \\ (m^3/s) \\ Q_{\rm min} & {\rm minimum$									
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$\begin{array}{cccc} C_{\rm s} & {\rm coefficient in Eq. (2) (m^2)} & X_{\rm m}, X_{\rm p} & {\rm dimensionless grinding variable, defined in Eqs} \\ d_{\rm h} & {\rm perforated hole diameter (m)} & (18) and (21), respectively & \gamma & {\rm control volume angle (rad)} \\ f_{\rm c} & {\rm centrifugal force acting on a unit volume of} & {\rm coolant (M/m^3)} & \gamma & {\rm control volume angle (rad)} \\ g_{\rm g} & {\rm gravitational constant (m/s^2)} & {\rm \rho} & {\rm coolant density (kg/m^3)} \\ h & {\rm equivalent liquid layer thickness in Eq. (2) (m)} \\ l & {\rm break-up length of a liquid jet in Eq. (A1) (m)} \\ N & {\rm total number of segments in a segmented wheel} \\ n_{\rm ch} & {\rm number of segments in a segmented wheel} \\ n_{\rm ch} & {\rm number of segmenta (kg/m^3)} \\ Oh & Ohnesorge number, Eq. (A3), (Oh=\mu/(\rho \sigma d_1)^{0.5}) \\ P & {\rm pumping power (W)} \\ P^* & {\rm power number, Eq. (21), (Q/R^3\omega)} \\ Q & {\rm total coolant flow rate (m^3/s)} \\ Q & {\rm mist flow rate (m^3/s)} \\ Q^* & {\rm mist flow rate (m^3/s)} \\ Q^m_{\rm max} & {\rm maximum coolant flow rate required in Eq. (27)} \\ m^m_{\rm minimum coolant flow rate required in Eq. (27)} \\ m^m_{\rm minimum coolant flow rate required in Eq. (27)} \\ m^m_{\rm minimum coolant flow rate required in Eq. (27)} \\ m^m_{\rm minimum coolant flow rate required in Eq. (27)} \\ m^m_{\rm minimum coolant flow rate required in Eq. (27)} \\ m^m_{\rm minimum coolant flow rate required in Eq. (27)} \\ m^m_{\rm minimum coolant flow rate required in Eq. (27)} \\ m^m_{\rm minimum coolant flow rate required in Eq. (27)} \\ m^m_{\rm minimum coolant flow rate required in Eq. (27)} \\ m^m_{\rm minimum coolant flow rate required in Eq. (27)} \\ m^m_{\rm minimum coolant flow rate required in Eq. (27)} \\ m^m_{\rm minimum coolant flow rate required in Eq. (27)} \\ m^m_{\rm minimum coolant flow rate required in Eq. (27)} \\ m^m_{\rm minimum coolant flow rate required in Eq. (27)} \\ m^m_{\rm minimum coolant flow rate required in Eq. (27)} \\ m^m_{\rm minimum coolant flow rate required in Eq. (27)} \\ m^m_{\rm minimum coolant flow rate required in Eq. (27)} \\ m^m_{\rm minimum coolant flow rate required in Eq.$	-	$(1/m^4)$	10						
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$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$C_{\rm s}$	coefficient in Eq. $(2)$ $(m^2)$	$X_{\rm m}, X_{\rm p}$	dimensionless grinding variable, defined in Eqs.					
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$\begin{array}{ccc} \operatorname{coolant}(N/m^3) & (kg/m^3) \\ g & \operatorname{gravitational constant}(m/s^2) & \rho & \operatorname{coolant density}(kg/m^3) \\ h & \operatorname{equivalent liquid layer thickness in Eq. (2) (m) \\ h & \operatorname{equivalent liquid layer thickness in Eq. (2) (m) \\ l & \operatorname{break-up length} of a liquid jet in Eq. (A1) (m) \\ r & \operatorname{surface tension}(N/m) \\ N & \operatorname{total number of segments in a segmented wheel \\ number of perforated holes within the coolant \\ chamber (Fig. 5) & \omega \\ minimum pumping power standard (kg/m^3) \\ Oh & Ohnesorge number, Eq. (A3), (Oh = \mu/(\rho\sigma d_1)^{0.5}) \\ P & pumping power (W) \\ P^{min} & minimum pumping power required (W) \\ P^{min} & power number, (P/\rho R^5 \omega^3) & pressure (Pa) \\ Q & \operatorname{total coolant flow rate supplied to a system } (m^3/s) & ch \\ Q_m & mist flow rate (m^3/s) & h \\ Q_m & mist flow rate (m^3/s) & k \\ Q_m & mist flow rate ratio in Eq. (21) & m \\ Q_m & mist flow rate ratio in Eq. (21) & m \\ Q_m & mist flow rate ratio in Eq. (21) & m \\ Q_m & minimum coolant flow rate required in Eq. (27) \\ (m^3/s) & p \\ Q_{max} & maximum coolant flow rate required in Eq. (27) \\ (m^3/s) & p \\ Q_{max} & minimum coolant flow rate required in Eq. (27) \\ (m^3/s) & p \\ Q_{max} & minimum coolant flow rate required in Eq. (27) \\ (m^3/s) & p \\ Q_{max} & minimum coolant flow rate required in Eq. (27) \\ (m^3/s) & p \\ Q_{max} & minimum coolant flow rate required in Eq. (27) \\ (m^3/s) & p \\ Q_{max} & minimum coolant flow rate required in Eq. (27) \\ (m^3/s) & p \\ Q_{max} & minimum coolant flow rate required in Eq. (27) \\ (m^3/s) & p \\ Q_{max} & minimum coolant flow rate required in Eq. (27) \\ (m^3/s) & p \\ Q_{max} & minimum coolant flow rate required in Eq. (27) \\ (m^3/s) & p \\ Q_{max} & minimum coolant flow rate required in Eq. (27) \\ (m^3/s) & p \\ Q_{max} & minimum coolant flow rate required in Eq. (27) \\ (m^3/s) & p \\ Q_{max} & minimum coolant flow rate required in Eq. (27) \\ (m^3/s) & p \\ Q_{max} & minimum coolant flow rate required in Eq. (27) \\ (m^3/s) & p \\ Q_{max} & minimum coolant flow rate required in Eq. (27) \\ (m^3/s) & p \\ Q_{max} & mini$	$d_1$	break-up diameter of a liquid jet in Eq. (A1) (m)	$\gamma$	control volume angle (rad)					
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# 2. Pumping power

# 2.1. Dimensional analysis

As shown in Figs. 1 and 2, the coolant layer, due to the wheel rotation,  $\omega$ , is forced to penetrate into the wheel-workpiece contact zone by a power, *P*, determined as [2]

$$P = \left(\frac{1}{2}\rho R\omega\right) C_{\rm s} \left(\sum_{k=1}^{n_{\rm cv}} v_{ik}\right)^2,\tag{1}$$

where *R* is the wheel radius,  $\rho$  is the coolant density, and *C*<sub>s</sub> is the coefficient representing the influence of the wheel configuration, defined as



Fig. 1. Penetration of coolant into a grinding zone.



Fig. 2. Analytical control volume

$$C_{\rm s} = \frac{1}{b} \left(\frac{\pi d_{\rm h}^2}{4}\right)^2 \left(\frac{2R}{h} - 1\right),\tag{2}$$

where *b* is the wheel width,  $d_h$  is the perforated hole diameter, *h* is the equivalent thickness of a coolant layer in the wheel-workpiece contact zone [2], and  $n_{cv}$  is the number of the coolant jets within the control volume, defined as

$$n_{\rm cv} = \frac{N\gamma}{2\pi},\tag{3}$$

in which N is the total number of the segments fitted in a wheel and  $\gamma$  is the control volume angle, a function of the viscosity,  $\mu$ , and surface tension,  $\sigma$ , i.e.

$$\gamma = \gamma(\mu, \sigma). \tag{4}$$

In Eq. (1),  $v_{ik}$  is the velocity of a coolant jet, which, according to the continuity law, can be expressed in term of the individual flow rate of coolant through a hole,  $Q_{ik}$ , as

$$v_{ik} = \frac{4Q_{ik}}{\pi d_{\rm h}^2}.\tag{5}$$

On the other hand,  $v_{ik}$  can be written as, following the energy equation,

$$v_{ik} = v_2 = \left[v_1^2 + 2\varDelta_z \left(g + \frac{f_c}{\rho}\right) + \frac{\varDelta p}{\rho}\right]^{1/2} \tag{6}$$

where  $v_1$  is the initial velocity at plane 1,  $\Delta z = z_1 - z_2$  is the perforated hole length,  $\Delta p = p_1 - p_2$  is the pressure drop through a hole (Fig. 3) and  $f_c = \rho R \omega^2$  is the centrifugal force acting on a unit coolant volume.

It should be mentioned that to reduce the excessive number of cutting edges and their undesirable friction with the workpiece [2], the segmented wheel is often designed to posses more than one coolant jet within the control volume, i.e.  $n_{\rm cv} > 1$ , as shown in Fig. 1. However, due to the wheel rotation, the distributions of coolant flow rates,  $Q_{ik}$ , and hence the coolant jet velocity  $v_{ik}$  over the entire control volume are not uniform, as shown in Fig. 4.

Hence, to obtain a quantitative prediction, the pumping power P should be expressed as



Fig. 3. Flow of a coolant jet.

$$P = P(\rho, \mu, \sigma, R, N, d_{\rm h}, b, h, \Delta z, \gamma, \omega, \Delta p, v_{ik})$$
(7)

Since the influence of  $f_c$  in Eq. (6) has been implicitly taken into account by the combination of  $\rho$ , R and  $\omega$ , the effect of pressure drop  $\Delta p$  can be considered at the static condition where  $\omega = 0$ . In the case with a coolant chamber as shown in Fig. 5, the equations of Bernoulli and continuity can be applied to planes 1 and 2, to determine the mean static pressure drop,  $\Delta \bar{p}_o$ , through the perforated holes, which results in [4]

$$\Delta \bar{p}_{\rm o} = \frac{Q^2 \rho}{2} \left( \frac{A_1^2 - A_2^2}{A_1^2 A_2^2} \right) = C_{\rm f} \left( \frac{Q^2 \rho}{2} \right) \tag{8}$$

where Q is the total coolant flow rate supplied to the system and  $C_f = (A_1^2 - A_2^2)/A_1^2 A_2^2$  is a coefficient representing the influence of the chamber design on  $\Delta \bar{p}_0$ , in which  $A_1$  and  $A_2$ are the inner cross-sectional area of the fluid chamber and the total cross-sectional area of the perforated holes within the chamber, respectively. If the number of the perforated holes within the chamber is  $n_{ch}$  and the internal width of the chamber is  $b_{ch}$ ,  $A_1$  and  $A_2$  can be derived as

$$A_1 = 2\pi R \frac{n_{\rm ch}}{N} b_{\rm ch},\tag{9}$$

and

$$A_2 = n_{\rm ch} \frac{\pi d_h^2}{4} \tag{10}$$

Eqs. (8)–(10) can also be applied to the case when coolant is introduced to the wheel by the free-flow method (Fig. 3b). In this case,

$$(n_{\rm ch})_{\rm free-flow} = N \tag{11}$$

and

$$b_{\rm r} = b_{\rm ch} \tag{12}$$

where  $b_{\rm r}$  is the width of the inner wheel rim.

Fluid chamber b) a)

Fig. 4. Coolant flow profiles: (a) free-flow method, and (b) forced flow method.

With the above analytical relationships of the variables in mind, we can simplify Eq. (7) to

$$P = P(\rho, \mu, \sigma, C_{\rm f}, R, b, h, \omega, Q) \tag{13}$$

Then the Buckingham  $\Pi$  theorem [17,18] allows the relationship to be expressed as

$$f(\pi_1, \pi_2, \pi_3, \pi_4, \pi_5, \pi_6, \pi_7) = 0 \tag{14}$$

where

 $\pi_1 = \frac{P}{\rho R^5 \omega^3} = P^*$ , is the power number representing the pumping power achieved;

 $\pi_2 = \frac{\rho R^2 \omega}{\mu}$  = Re, is the Reynolds number representing the effect of viscosity;

 $\pi_3 = \frac{\rho R^3 \omega^2}{\sigma}$  = We, is the Weber number representing the effect of surface tension;

 $\pi_4 = C_f R^4$ , standing for the influence of method of introducing coolant into the segmented wheel system;

 $\pi_5 = \frac{Q}{R^3 \omega} = Q^*$ , representing the effect of coolant flow rate supplied to the system;

 $\pi_6 = \frac{b}{R}$ , representing the effect of wheel width; and  $\pi_7 = \frac{b}{R}$ , representing the combination effect of the wheel specification and the grinding depth of cut.

For a given segmented wheel system,  $\pi_4$ ,  $\pi_6$  and  $\pi_7$  can be reconciled, i.e.

$$\pi_{4,6,7} = \pi_4 \pi_6 \pi_7 = C_{\rm f} b h R^2 = C_{\rm fw}^* \tag{15}$$



Fig. 5. Schematic of the coolant flow through the holes.

which can be considered as a geometrical influence number to represent the combination effects of  $\pi_4$ ,  $\pi_6$  and  $\pi_7$  of the system.

Hence, Eq. (14) can be rewritten as

$$P^* = f_1(\text{Re}, \text{We}, C^*_{\text{fw}}, Q^*)$$
 (16)

The power law of dimensional analysis [19] is used to express Eq. (16) in a form,

$$P^* = C_{\rm p} X_{\rm p} \tag{17}$$

where  $C_p$  is a correlation coefficient, and

$$X_{\rm p} = {\rm Re}^m W e^n (C_{\rm fw}^*)^q (Q^*)^r.$$
(18)

# 2.2. Experimental verification

The component of  $\left(\sum_{k=1}^{n_{cv}} v_{ik}\right)$  in Eq. (1) can be experimentally determined using the method described in the Appendix at the end of the paper. These values are used to compute the magnitudes of dependent parameter  $P^*$  in Eq. (17), which, together with the parameters in Eq. (18), gives the result shown in Fig. 6. Within the range of Re and We covering many practical grinding operations with waterbased coolants<sup>1</sup>

$$7.3 \times 10^{5} \le \text{Re} \le 4.6 \times 10^{6}$$

and

$$7.1 \times 10^4 \le \text{We} \le 2.2 \times 10^6$$
, (19)

the relation below is obtained using the method of multivariable regression,

$$P^* = 47.8 \text{Re}^{-0.17} \text{We}^{-0.42} (C^*_{\text{fw}})^{0.25} (Q^*)^{1.02}$$
(20)

Eq. (20) is capable for predicting the power number  $P^*$ . Since wheel speed  $\omega$  is included in the dimensionless parameters  $P^*$ , Re, We and  $Q^*$ , when Eqs. (17) and (18) are rearranged with  $\omega$  as an explicit variable, a term of  $\omega^{0.97}$  will

<sup>&</sup>lt;sup>1</sup> The maximum and minimum values of Re and We in this range are associated with the grinding conditions below: (a) Wheel speed varies from 6.0 to 28.0 m/s which is 85% of the safety limit using a conventional wheel with high strength CBN vitrified bonded [20]; and (b) The concentration of the water-based coolant (Noritake SA-02) varies from 1:60 to 1:85, whose viscous properties are shown in Table 1.



Fig. 6. Pumping power correlation.

appear in the right hand side of Eq. (7). This means that a high wheel speed enhances the pumping power, which is in agreement with the conclusion in Part 1 of this series study [2]. Eq. (20) also shows, by referring to Eqs. (17) and (18), that pumping power is a strong function of the total coolant flow rate (r=1.02) and its effectiveness depends very much on the coolant chamber characteristic (q=0.25). With a given grinding condition, a higher pumping power can be obtained when coolant is pressurised (un-filled dots in Fig. 6).

# 3. Practical implications

#### 3.1. Environmental consideration

In the analysis of the mist flow rate generated by a segmented wheel [4], the authors have proposed a formula to predict the mist flow rate ratio  $Q_{\rm m}^*$ , i.e.

$$Q_{\rm m}^* = \frac{Q_{\rm m}}{Q} = C_{\rm m} X_{\rm m} \tag{21}$$

where

 $C_{\rm m} = 45.2 \times 10^{-3}$ and

$$X_{\rm m} = {\rm Re}^{0.06} {\rm We}^{0.18} \left(\frac{C_{\rm f} Q^2}{2\omega^2 R^2}\right)^{0.08} (\cos \phi)^{2.26}$$

in which  $Q_{\rm m}$  is the mist flow rate and  $\phi$  is the angular position of the chamber (Fig. 4b).

The plot of Eq. (21) is illustrated in Fig. 7. In comparison with Eq. (20), it is found that an increase of the coolant viscosity and surface tension, which reduces Reynolds and Weber numbers, will improve coolant penetration and reduce mist. However, the viscous properties depend on the chemical additives in coolant whose use should be minimised in practice to reduce the cost of waste disposal [21,22]. Unfortunately, it can be seen that an adjustment of

grinding variables to improve coolant penetration based on Eq. (20) (e.g. increasing  $\omega$  and Q) will lead to a high mist formation rate according to Eq. (21). Hence, to determine a set of optimal grinding parameters and coolant selection, ( $\rho$ ,  $\mu$ , $\sigma$ , $\omega$ ,Q)<sub>op</sub> that satisfies both the desired mist flow rate and pumping power, Eqs. (21) and (22) must be solved simultaneously, i.e.

$$(\rho, \mu, \sigma, \omega, Q)_{\rm op} = (\rho, \mu, \sigma, \omega, Q)_{\rm p} \cap (\rho, \mu, \sigma, \omega, Q)_{\rm m}$$
(22)

where  $(\rho,\mu,\sigma,\omega,Q)_p$  is the solution of Eq. (20) aiming at the highest pumping power and  $(\rho,\mu,\sigma,\omega,Q)_m$  is that of Eq. (21) aiming at the lowest mist flow rate.

To determine the solution of Eq. (22), the constraints must be set based on a given grinding case, which is specified by the limitation of the coolant supply, safety limit of wheel speed, and the limited rate of mist. This will be demonstrated in the example below.

# 3.2. Example

The grinding conditions are listed in Table 1. With a given grinding wheel system and coolant type, the wheel



Fig. 7. Mist flow rate correlation.

Table 1 Experimental parameters

Grinding machine	Minini Junior 90 CNC-M286		
Grinding wheel	Designation: B100P120V		
	Radius, $R = 150 \text{ mm}, 144$		
	segments		
	Perforated hole diameter,		
	$d_{\rm h} = 2  {\rm mm}$		
	Hole length, $(z_1 - z_2) = 5 \text{ mm}$		
	Allowable wheel speed = 28.1 m/s		
Fluid chamber	Cross sectional area, $A_1 = 88$ .		
	3 mm <sup>2</sup>		
	Number of perforated holes within		
	the fluid chamber, $n=4$		
Grinding parameters	- Specific grinding energy: $u_g = 57$ .		
	5 J/m <sup>3</sup> [28]		
	- Table speed: 5 mm/s		
	- Depths of cut: 25 μm		
Coolant	Noritake SA-02		
	Coolant density: $\rho = 980 \text{ kg/m}^3$		
	Density of chemical additive,		
	$\rho_{\rm a} = 975 \text{ kg/m}^3$		
	Concentration:		
	1:60 ( $\mu = 12.1 \times 10^{-4}$ Ns/m <sup>2</sup> ,		
	$\sigma = 73.1 \times 10^{-3} \text{ N/m}$		
	1:85 ( $\mu$ =8.9×10 <sup>-4</sup> Ns/m <sup>2</sup> ,		
	$\sigma = 73.1 \times 10^{-3} \text{ N/m}$		

speed ( $\omega$ ) and coolant supply flow rate (*Q*) are the two parameters to be determined for the optimisation. Eq. (22) therefore becomes

$$(\omega, Q)_{\rm op} = (\omega, Q)_{\rm p} \cap (\omega, Q)_{\rm m} \tag{23}$$

The grinding constraints are:

$$P \ge P_{\min},\tag{24}$$

$$Q_{\rm m} \le Q_{\rm m,max},\tag{25}$$

and

$$\omega \le \omega_{\max} \tag{26}$$

where  $P_{\min}$  is the minimum pumping power required for a satisfactory grinding without thermal damage,  $Q_{m,\max}$  is the maximum mist flow rate allowed by an environmental legislation and  $\omega_{\max}$  is the safety limit of rotational wheel speed.

The minimum pumping power required for grinding of 1045 steel at depth of cut = 25  $\mu$ m has been given in Part 1 of this study [2], i.e.  $P_{\min}$  = 1.25 W.

On the other hand, according to the National Occupational Health and Safety Commission (NOHSC) [23], the contamination of inspirable particles in the atmospheric air must not exceed an occupational exposure standard,  $OES = 5 \text{ mg/m}^3$ .

Based on this, the maximum allowable mist flow rate can be found to be  $Q_{m,max} = 3.1 \times 10^{-5} \text{ m}^3/\text{s}$ , using the methods given by Refs. [6,23,24]. In the calculation, it was assumed that the ventilation rate of the grinding room was 0. 047 m<sup>3</sup>/s, which is similar to that of an ordinary kitchen [25], the reference period of mist sampling was 8 h, and the volume of the grinding room was 500 m<sup>3</sup>.

With the  $P_{\min}$  and  $Q_{m,\max}$  ready above, it is now possible to determine  $(\omega, Q)_{op}$  in Eq. (23). By substituting the value of  $P_{\min}$  into Eq. (20), a minimum coolant flow rate,  $Q_{\min}$ , can be determined. At the same time, the maximum coolant flow rate  $Q_{\max}$  controlled by Eq. (21), can also be determined by substituting the value of  $Q_{m,\max}$ . The optimised flow rate must be within the range

$$Q_{\max} \ge Q \ge Q_{\min},\tag{27}$$

to ensure a sufficient coolant quantity for the satisfactory grinding and a mist flow rate below the limit. The calculation procedure is shown Fig. 8.

Some numerical results are listed in Table 2. It appears that when a wheel speed is below 1200 rpm,  $Q_{\text{max}} < Q_{\text{min}}$ .



Fig. 8. Optimisation process.

Table 2 Optimisation results

$\omega$ (rpm)	Re ( $\times 10^{6}$ )	We ( $\times 10^{5}$ )	Q <sub>min</sub> (L/ min)	Q <sub>max</sub> (L/ min)
700	1.3	2.4	5.4	3.5
1000	1.9	5.0	3.8	3.2
1200	2.3	7.1	3.2	3.1
1450	2.8	10.4	2.7	3.0
1785	3.4	15.8	2.2	2.8

This is not reasonable and indicates that in this case, a higher ventilation rate must be provided to remove the harmful mist more quickly. The optimal condition  $(\omega, Q)_{op}$  is found to be  $\omega = 1785$  rpm at which  $Q_{max} = 2.8$  L/min being slightly higher than  $Q_{min} = 2.2$  L/min, indicating that the operation consumes less coolant.

The above optimisation process can be also applied to different selections of coolant types with Re and We numbers in the valid range.

# 3.3. Conclusions

A parametric model has been developed to predict the power of coolant penetration into the grinding zone with the application of a segmented wheel. Experimental data were found to be in reasonable agreement with the prediction.

By coupling with the mist formation analysis, the developed model offers a control guideline for the optimal use of grinding coolants in achieving a balanced consideration of process productivity and environmental consciousness.

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# Appendix

# Determination of v<sub>ik</sub>

According to the Weber theory [6,8] for the instability of Newtonian jets, when a liquid jet subjected to the forces of surface tension and inertia,

$$\frac{l}{d_1} = \ln\left(\frac{d_1}{2\delta}\right) \operatorname{We}_l^{0.5}(1+3\mathrm{Oh}) \tag{A1}$$

where  $\delta$  is the amplitude of disturbance; l and  $d_l$  are the break-up length and diameter of a liquid jet, respectively (Figs. 4a and b) which can be determined using the method of high speed strobe photography [4]; We and Oh is

the Weber and Ohnesorge number, respectively, defined as

$$We_{l} = \frac{\rho d_{l} v_{ik}^{2}}{\sigma}$$
(A2)

$$Oh = \frac{\mu}{(\rho \sigma d_1)^{0.5}} \tag{A3}$$

The parameter  $\ln(d_1/2\delta)$  depends on the nature of the jet, i.e. laminar or turbulent, which is determined by the following conditions [26]:

 $Re_1 < Re_c$ : laminar flow  $Re_1 > Re_c$ : turbulent flow

where

$$\operatorname{Re}_{l} = \frac{\rho v_{ik} d_{l}}{\mu} \tag{A4}$$

and Rec is the critical Reynolds number, defined as

$$\operatorname{Re}_{c} = 1.2 \times 10^{4} \left(\frac{1}{d_{1}}\right)^{-0.3}$$
 (A5)



Fig. A1. Steps for determining of  $v_1$ .

For a laminar flow, according to Grant et al. [27]:

$$\ln\left(\frac{d_1}{2\delta}\right) = 7.68 - 2.66\text{Oh},\tag{A6}$$

but for a turbulent flow, Eq. (A1) becomes [27]

$$\frac{l}{d_1} = 8.51 \,\mathrm{We}_1^{0.32} \tag{A7}$$

Now,  $v_{ik}$  can be determined following the steps shown in Fig. A1.

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